



**Mathematics
Higher level
Paper 1**

Thursday 4 May 2017 (afternoon)

Candidate session number

2 hours

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Instructions to candidates

- Write your session number in the boxes above.
- Do not open this examination paper until instructed to do so.
- You are not permitted access to any calculator for this paper.
- Section A: answer all questions. Answers must be written within the answer boxes provided.
- Section B: answer all questions in the answer booklet provided. Fill in your session number on the front of the answer booklet, and attach it to this examination paper and your cover sheet using the tag provided.
- Unless otherwise stated in the question, all numerical answers should be given exactly or correct to three significant figures.
- A clean copy of the **mathematics HL and further mathematics HL formula booklet** is required for this paper.
- The maximum mark for this examination paper is **[100 marks]**.

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3. [Maximum mark: 5]

Solve the equation $\sec^2 x + 2 \tan x = 0$, $0 \leq x \leq 2\pi$.

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Section B

Answer **all** questions in the answer booklet provided. Please start each question on a new page.

10. [Maximum mark: 15]

The continuous random variable X has a probability density function given by

$$f(x) = \begin{cases} k \sin\left(\frac{\pi x}{6}\right), & 0 \leq x \leq 6 \\ 0, & \text{otherwise.} \end{cases}$$

(a) Find the value of k . [4]

(b) By considering the graph of f write down

(i) the mean of X ;

(ii) the median of X ;

(iii) the mode of X . [3]

(c) (i) Show that $P(0 \leq X \leq 2) = \frac{1}{4}$.

(ii) Hence state the interquartile range of X . [6]

(d) Calculate $P(X \leq 4 | X \geq 3)$. [2]



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11. [Maximum mark: 17]

(a) (i) Express $x^2 + 3x + 2$ in the form $(x + h)^2 + k$.

(ii) Factorize $x^2 + 3x + 2$.

[2]

Consider the function $f(x) = \frac{1}{x^2 + 3x + 2}$, $x \in \mathbb{R}$, $x \neq -2$, $x \neq -1$.

(b) Sketch the graph of $f(x)$, indicating on it the equations of the asymptotes, the coordinates of the y -intercept and the local maximum.

[5]

(c) Show that $\frac{1}{x+1} - \frac{1}{x+2} = \frac{1}{x^2 + 3x + 2}$.

[1]

(d) Hence find the value of p if $\int_0^1 f(x) dx = \ln(p)$.

[4]

(e) Sketch the graph of $y = f(|x|)$.

[2]

(f) Determine the area of the region enclosed between the graph of $y = f(|x|)$, the x -axis and the lines with equations $x = -1$ and $x = 1$.

[3]



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12. [Maximum mark: 18]

Consider the polynomial $P(z) = z^5 - 10z^2 + 15z - 6$, $z \in \mathbb{C}$.

(a) Write down the sum and the product of the roots of $P(z) = 0$. [2]

(b) Show that $(z - 1)$ is a factor of $P(z)$. [2]

The polynomial can be written in the form $P(z) = (z - 1)^3(z^2 + bz + c)$.

(c) Find the value of b and the value of c . [5]

(d) Hence find the complex roots of $P(z) = 0$. [3]

Consider the function $q(x) = x^5 - 10x^2 + 15x - 6$, $x \in \mathbb{R}$.

(e) (i) Show that the graph of $y = q(x)$ is concave up for $x > 1$.

(ii) Sketch the graph of $y = q(x)$ showing clearly any intercepts with the axes. [6]



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