



**Mathematics  
Higher level  
Paper 2**

Friday 5 May 2017 (morning)

Candidate session number

2 hours

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**Instructions to candidates**

- Write your session number in the boxes above.
- Do not open this examination paper until instructed to do so.
- A graphic display calculator is required for this paper.
- Section A: answer all questions. Answers must be written within the answer boxes provided.
- Section B: answer all questions in the answer booklet provided. Fill in your session number on the front of the answer booklet, and attach it to this examination paper and your cover sheet using the tag provided.
- Unless otherwise stated in the question, all numerical answers should be given exactly or correct to three significant figures.
- A clean copy of the **mathematics HL and further mathematics HL formula booklet** is required for this paper.
- The maximum mark for this examination paper is **[100 marks]**.

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3. [Maximum mark: 6]

The coefficient of  $x^2$  in the expansion of  $\left(\frac{1}{x} + 5x\right)^8$  is equal to the coefficient of  $x^4$  in the expansion of  $(a + 5x)^7$ ,  $a \in \mathbb{R}$ . Find the value of  $a$ .

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### Section B

Answer **all** questions in the answer booklet provided. Please start each question on a new page.

9. [Maximum mark: 8]

The times taken for male runners to complete a marathon can be modelled by a normal distribution with a mean 196 minutes and a standard deviation 24 minutes.

- (a) Find the probability that a runner selected at random will complete the marathon in less than 3 hours. [2]

It is found that 5% of the male runners complete the marathon in less than  $T_1$  minutes.

- (b) Calculate  $T_1$ . [2]

The times taken for female runners to complete the marathon can be modelled by a normal distribution with a mean 210 minutes. It is found that 58% of female runners complete the marathon between 185 and 235 minutes.

- (c) Find the standard deviation of the times taken by female runners. [4]

10. [Maximum mark: 15]

In triangle PQR,  $PR = 12$  cm,  $QR = p$  cm,  $PQ = r$  cm and  $\hat{Q}PR = 30^\circ$ .

- (a) Use the cosine rule to show that  $r^2 - 12\sqrt{3}r + 144 - p^2 = 0$ . [2]

Consider the possible triangles with  $QR = 8$  cm.

- (b) Calculate the two corresponding values of  $PQ$ . [3]

- (c) Hence, find the area of the smaller triangle. [3]

Consider the case where  $p$ , the length of  $QR$  is not fixed at 8 cm.

- (d) Determine the range of values of  $p$  for which it is possible to form two triangles. [7]



Do **not** write solutions on this page.

11. [Maximum mark: 9]

Xavier, the parachutist, jumps out of a plane at a height of  $h$  metres above the ground. After free falling for 10 seconds his parachute opens.

His velocity,  $v \text{ ms}^{-1}$ ,  $t$  seconds after jumping from the plane, can be modelled by the function

$$v(t) = \begin{cases} 9.8t, & 0 \leq t \leq 10 \\ \frac{98}{\sqrt{1 + (t - 10)^2}}, & t > 10 \end{cases} .$$

(a) Find his velocity when  $t = 15$ . [2]

(b) Calculate the vertical distance Xavier travelled in the first 10 seconds. [2]

His velocity when he reaches the ground is  $2.8 \text{ ms}^{-1}$ .

(c) Determine the value of  $h$ . [5]

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12. [Maximum mark: 18]

Consider  $f(x) = -1 + \ln(\sqrt{x^2 - 1})$ .

(a) Find the largest possible domain  $D$  for  $f$  to be a function. [2]

The function  $f$  is defined by  $f(x) = -1 + \ln(\sqrt{x^2 - 1})$ ,  $x \in D$ .

(b) Sketch the graph of  $y = f(x)$  showing clearly the equations of asymptotes and the coordinates of any intercepts with the axes. [3]

(c) Explain why  $f$  is an even function. [1]

(d) Explain why the inverse function  $f^{-1}$  does not exist. [1]

The function  $g$  is defined by  $g(x) = -1 + \ln(\sqrt{x^2 - 1})$ ,  $x \in ]1, \infty[$ .

(e) Find the inverse function  $g^{-1}$  and state its domain. [4]

(f) Find  $g'(x)$ . [3]

(g) Hence, show that there are no solutions to

(i)  $g'(x) = 0$ ;

(ii)  $(g^{-1})'(x) = 0$ . [4]

