



**Mathematics  
Higher level  
Paper 2**

Thursday 3 May 2018 (morning)

Candidate session number

2 hours

--	--	--	--	--	--	--	--	--	--

**Instructions to candidates**

- Write your session number in the boxes above.
- Do not open this examination paper until instructed to do so.
- A graphic display calculator is required for this paper.
- Section A: answer all questions. Answers must be written within the answer boxes provided.
- Section B: answer all questions in the answer booklet provided. Fill in your session number on the front of the answer booklet, and attach it to this examination paper and your cover sheet using the tag provided.
- Unless otherwise stated in the question, all numerical answers should be given exactly or correct to three significant figures.
- A clean copy of the **mathematics HL and further mathematics HL formula booklet** is required for this paper.
- The maximum mark for this examination paper is **[100 marks]**.

CLASES DE MATEMÁTICAS Y FÍSICA  
BACHILLERATO INTERNACIONAL  
WHATSAPP +51976438482  
WWW.TEOTEVES.COM





















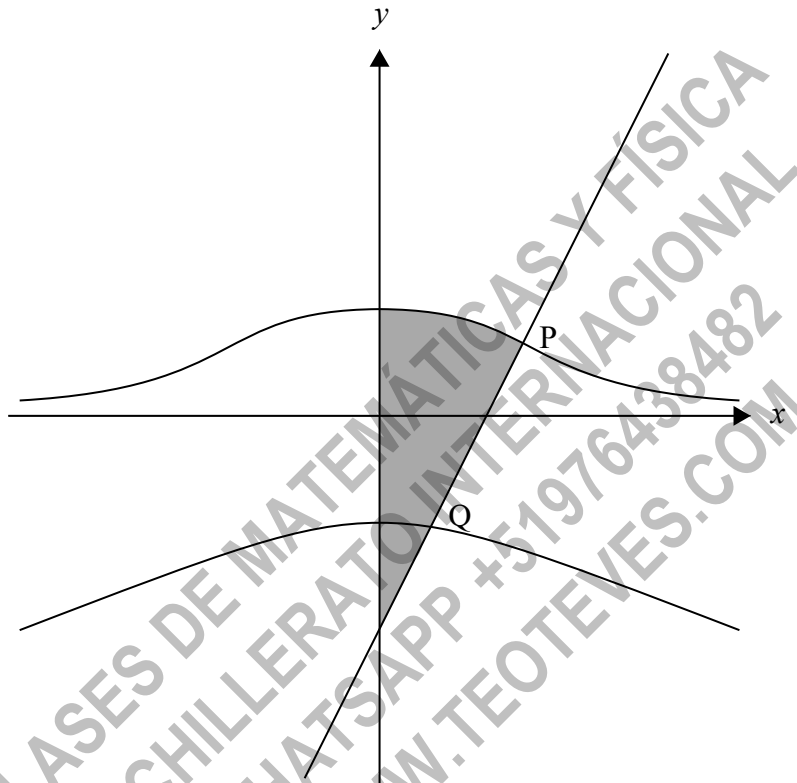
Do **not** write solutions on this page.

**Section B**

Answer **all** questions in the answer booklet provided. Please start each question on a new page.

9. [Maximum mark: 22]

The following graph shows the two parts of the curve defined by the equation  $x^2y = 5 - y^4$ , and the normal to the curve at the point  $P(2, 1)$ .



- (a) Show that there are exactly two points on the curve where the gradient is zero. [7]
- (b) Find the equation of the normal to the curve at the point  $P$ . [5]
- (c) The normal at  $P$  cuts the curve again at the point  $Q$ . Find the  $x$ -coordinate of  $Q$ . [3]
- (d) The shaded region is rotated by  $2\pi$  about the  $y$ -axis. Find the volume of the solid formed. [7]



12EP10

Do **not** write solutions on this page.

10. [Maximum mark: 13]

The continuous random variable  $X$  has probability density function  $f$  given by

$$f(x) = \begin{cases} 3ax & , 0 \leq x < 0.5 \\ a(2 - x) & , 0.5 \leq x < 2 \\ 0 & , \text{otherwise} \end{cases}$$

- (a) Show that  $a = \frac{2}{3}$ . [3]
- (b) Find  $P(X < 1)$ . [3]
- (c) Given that  $P(s < X < 0.8) = 2 \times P(2s < X < 0.8)$ , and that  $0.25 < s < 0.4$ , find the value of  $s$ . [7]

CLASES DE MATEMÁTICAS Y FÍSICA  
BACHILLERATO INTERNACIONAL  
WHATSAPP +51976438482  
WWW.TEOTEVES.COM



12EP11

Do **not** write solutions on this page.

11. [Maximum mark: 15]

Two submarines A and B have their routes planned so that their positions at time  $t$  hours,

$0 \leq t < 20$ , would be defined by the position vectors  $\mathbf{r}_A = \begin{pmatrix} 2 \\ 4 \\ -1 \end{pmatrix} + t \begin{pmatrix} -1 \\ 1 \\ -0.15 \end{pmatrix}$  and

$\mathbf{r}_B = \begin{pmatrix} 0 \\ 3.2 \\ -2 \end{pmatrix} + t \begin{pmatrix} -0.5 \\ 1.2 \\ 0.1 \end{pmatrix}$  relative to a fixed point on the surface of the ocean (all lengths are in kilometres).

- (a) Show that the two submarines would collide at a point P and write down the coordinates of P. [4]

To avoid the collision submarine B adjusts its velocity so that its position vector is now given by

$$\mathbf{r}_B = \begin{pmatrix} 0 \\ 3.2 \\ -2 \end{pmatrix} + t \begin{pmatrix} -0.45 \\ 1.08 \\ 0.09 \end{pmatrix}.$$

- (b) (i) Show that submarine B travels in the same direction as originally planned. [3]  
 (ii) Find the value of  $t$  when submarine B passes through P.  
 (c) (i) Find an expression for the distance between the two submarines in terms of  $t$ .  
 (ii) Find the value of  $t$  when the two submarines are closest together.  
 (iii) Find the distance between the two submarines at this time. [8]

